

1 **Analysis of tidal amplitude changes using the EMD method**

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26 **Abstract:**

27 Empirical Mode Decomposition/Hilbert-Huang transformation (EMD/HHT) has been used for
28 various geophysical data, including analysis of sea level records to detect trends in sea level rise
29 (SLR) and decadal variations. However, application of EMD to high-frequency sea level
30 variability is less common, so it is tested here as a tool to analyze hourly sea level data and to
31 detect time-dependent changes in tidal amplitudes. The advantage of the EMD over a standard
32 Harmonic Analysis (HA) is that it can detect changes in tidal properties over time with one
33 calculation of an entire record, while HA will require multiple calculations over shorter
34 subsection records; here the two methods are compared. The highest and second-highest
35 frequency modes of the EMD represent the semi-diurnal and diurnal tides, respectively, with
36 especially high correlation between the variations of EMD first mode and M_2 tidal amplitude
37 obtained from HA. High agreements are obtained between HA and EMD mode 1 derived M_2
38 amplitude and validated by an independent regional tidal solution. The modulation of nodal cycle
39 estimated from EMD mode 1 is about 2-3% of M_2 tide amplitude. Moreover, the amplitude of
40 the M_2 tide seems to slowly increase over time in most stations along the U.S. East Coast
41 (probably due to SLR), but at some locations, such as Wilmington, NC, a much larger increase in
42 the M_2 tide is likely due to local morphological changes associated with sediment movements
43 and erosion. The analysis also shows some interannual variations in tidal amplitudes at some
44 locations that may relate to local man-made changes such as dredging or shoreline structures.

45 Keywords: tide, EMD, harmonic analysis, sea level

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48 **1. Introduction**

49 The U.S. Northeastern coast has been seen as a ‘hotspot’ of with acceleration in sea level rise
50 (SLR, Sallenger et al., 2012; Ezer and Corlett, 2012) and flooding (Ezer and Atkinson, 2014).
51 The region shows significantly higher trend than global mean SLR (Church and White, 2011;
52 Houston and Dean, 2011). This is due to a combination of land subsidence and potential
53 slowdown of the Atlantic Meridional Overturning Circulation (AMOC) and a weakening of the
54 Gulf Stream (GS) flow (Ezer et al., 2013; Ezer, 2015). SLR increases the damage to low-lying
55 coastal communities during storm surges (Tebaldi et al., 2012; Wahl et al., 2014; Wdowinski et
56 al., 2016) and also increase the frequency of minor tidal flooding (Ezer and Atkinson, 2014;
57 Sweet et al., 2014). Since minor flooding is directly related to the combination of SLR and tidal
58 amplitude, it is important to detect any changes in the characteristics of tides over time.

59 Recent studies have demonstrated the increases of the M_2 tidal amplitude in the Gulf of
60 Maine (Ray, 2006; 2009) and along the U.S. East Coast (Woodworth, 2010). Coherent linear
61 trends of tidal range in the last 30-90 years have been reported over the regions (Flick et al.,
62 2003). Müller et al. (2011) pointed out that the physical causes of tide trends and their spatial
63 variability are uncertain and it is difficult to relate them to other oceanic or atmospheric variables.
64 Future SLR can affect tides in coastal regions (Pelling et al., 2013). Numerical modeling
65 experiments of the impact of future SLR on tides demonstrate very different local response, so
66 that for the same SLR rate, tidal energy may increase on one coast and decrease in another
67 nearby coasts (Lee et al., 2016). Although the glacial isostatic adjustment and SLR contribute to
68 the trend of M_2 tidal amplitude, the numerical simulations could not reproduce the spatial pattern
69 of the tidal trend (Müller et al, 2011).

70 At some tide gauge locations, the changes in M_2 tidal amplitude are significant compared
71 with the SLR trend (Müller et al, 2011). This study motivated by the fact that considerable
72 variability of tides may increase the flooding risk when combined with the sea level rise
73 acceleration in the study area (Greenberg et al., 2012; Ezer and Atkinson, 2014), particularly for
74 the low-lying populated regions (e.g., Hampton Roads, south Florida, Miami Beach) vulnerable
75 to SLR (Zhang, 2011; Zhang and Sheng, 2013; Atkinson et al., 2013; Wdowinski et al., 2016).

76 One of the typical methods used to study the changes in tides is harmonic analysis (HA,
77 (Foreman, 1977) applied to hourly sea level records, though the impact of the sinusoidal nodal
78 cycle (18.61 years) need to be corrected (Müller et al, 2011). In this way, the trends and
79 variability of amplitude and phases of each semi-diurnal and diurnal tide constituents are
80 determined. Note however, that the changes in tidal characteristics due to SLR and other climatic
81 changes can be very different between one region to another (Woodworth, 2010).

82 In this work, we aim to study the possibility of using Empirical Mode Decomposition
83 (EMD) analysis (Huang et al., 1998, Huang and Wu, 2008) to describe the M_2 tidal amplitude
84 variability by comparing the EMD with that computed using standard HA. The EMD/HHT
85 method is especially useful for non-stationary and nonlinear time series, so that irregular patterns
86 of storm surges, or tidal amplitude changes over time are good test cases for this method. The
87 method decomposes any time series data into a finite number of intrinsic mode functions with
88 time-variable amplitudes and frequencies; the number of modes is determined by the length of
89 the record and the intrinsic variability of the time series. It has been widely used for analysis of
90 many kinds of geophysical data (Wu and Huang, 2009).

91 Recently, the method has been applied to calculate SLR trends and acceleration and long
92 term sea level variations (e.g., Ezer, 2013; 2015; Bonaduce et al., 2016; Ezer et al., 2016; Cheng

93 et al., 2016). The method was also used to sea level reconstruction (e.g., Sha et al., 2015) and
94 calculate future projections of local SLR based on extrapolation of past SLR rates and
95 acceleration (Ezer and Corlett, 2012). Here it is used to analyze the high-frequency modes to test
96 if they can describe the variability of the M_2 tidal amplitude. Note that because EMD is a non-
97 stationary method, it can detect time-dependent changes in amplitude and frequency with one
98 calculation of an entire record, while the HA will require multiple calculations, each one using a
99 small sub-sections of the data (say 1 year) to calculate how the tides changing over time. On the
100 other hand, the disadvantage of the EMD is that it is a non-parametric method (frequencies are
101 not specified) and thus it cannot guarantee to extract a particular tidal constituent. Therefore, the
102 proposed EMD analysis needs to be tested against standard methods.

103 The paper is organized as follows. The tide gauge sea level records and the methodology
104 employed in this study are described in section 2. The results are presented in section 3 and the
105 discussion and summary are provided in section 4.

106 **2. Dataset and methodology**

107 *a. Tide gauge sea level records*

108 In this study, hourly tide gauge data were downloaded from NOAA ([http://opendap.co-](http://opendap.co-ops.nos.noaa.gov/dods/)
109 [ops.nos.noaa.gov/dods/](http://opendap.co-ops.nos.noaa.gov/dods/)). Figure 1 shows the locations of the selected 17 tide gauges along the
110 U.S. coast. In Table 1, most stations provide long and continuous sea level records (average
111 starting year ~1917) except 2 stations in the lower Chesapeake Bay starting in the 1970s' (No. 10
112 and 11). The 2 shorter records are included because they are located in a region with significant
113 land subsidence (Kopp, 2013). Our study includes more stations than in a previous study of the
114 issue (Müller, 2011).

115 *b. Harmonic Analysis*

116 The standard tool for tidal analysis is usually based on HA; available software includes
117 for example, TASK (Tidal Analysis Software Kit, (Bell et al., 1996), T-tide (Pawlowicz et al.,
118 2002) and Utide (Codiga, 2011). The Utide was selected to calculate all tidal constituents for its
119 capability in solving the nodal cycle with the default settings. The HA is applied to data sections
120 over two adjacent calendar years (this reduces the effect of data gaps compared with a single
121 year analysis). Therefore, for a record over 1911-2016 for example, the HA is performed for the
122 periods 1911-1912, 1912-1913, ..., 2014-2015, 2015-2016. Experiments (not shown) with
123 averaging windows of 1, 2 or 3 years show very little effect on the results. Then the derived
124 variations of the M_2 tidal amplitude (with estimated errors on 95% confidence level) could be
125 used to compare with that computed from EMD method.

126 *c. Empirical Mode Decomposition*

127 To use EMD/HHT to detect changes in tidal amplitudes, we analyze the high frequency
128 modes obtained for each station. An EMD of a sea level record from location M (or from
129 regional mean) would be represented by

130
$$h^M(t) = \sum_{i=1}^N c_i^M(t) + r^M(t) \quad (1)$$

131 where N denotes a finite number, $c_i(t)$ is intrinsic oscillatory modes, and $r(t)$ is a residual “trend”.
132 Particular time dependent modes not necessarily represent specific processes, but the analysis
133 allows to evaluate relations between different data that may depend on different time scales.
134 Statistical confidence levels for EMD modes can be calculated using either a bootstrap method
135 (Ezer and Corlett, 2012) or ensemble simulations (Ezer et al., 2016). However, no quantitative
136 examination of each mode is done here, only the 2-year average magnitude of the peaks of the

137 highest frequency EMD mode is examined, to test if it is consistent with changed in the
138 amplitude of M_2 obtained by the HA. Appendix Figure A1 shows an example of the 19 EMD
139 modes for station Baltimore.

140 In order to keep the consistency between the EMD analysis and HA, we adopt the least-
141 square fitting method in Müller (2011) to remove the linear trend and the nodal cycle in EMD
142 first mode and HA results, i.e.,

$$143 \quad A_{M_2}(t) = A_0 + At + A_N \sin\left(\frac{2\pi}{18.5996}(t - 1973.66)\right) + A_N \cos\left(\frac{2\pi}{18.5996}(t - 1973.66)\right) \quad (2)$$

144 The trend term A and the cosine/sine nodal terms are removed (Woodworth, 2011; Mawdsley et
145 al., 2015), to reduce the effects of nodal cycle on M_2 tidal amplitude variations.

146 **3. Results**

147 Previous studies show that the tide gauge stations in the study area have mostly positive
148 trend in M_2 amplitude and negative trend at Newport (Müller et al., 2011), and the results
149 presented below are generally consistent with that study. Negative amplitude changes at
150 Chesapeake Bay Bridge Tunnel, Lewes and Sewells Point (Norfolk) are also shown in
151 Woodworth (2010). The largest and most interesting trend occurs at Wilmington, where the tide
152 gauge location upriver is strongly affected by sediment accumulation, as previously indicated
153 (Ray, 2009; Ezer and Atkinson, 2014).

154 Figure 2a shows the hourly sea level time series (m) estimated with EMD analysis (the
155 first mode, in blue). The black curve presents the M_2 amplitude estimated using HA (section 2b)
156 at Wilmington. The red curve denotes sea level variation magnitude of the EMD first mode,
157 which computed from the peaks of EMD first mode (section 2c). The difference in tidal
158 amplitude variation between the two methods is quite small (~5%) and mainly associated with

159 the 18.6 nodal cycle (Figure 2c), which is absent from the HA analysis (where only M_2
160 frequency is extracted), but still impact the EMD analysis if not explicitly removed.

161 Figures 2d-2f are similar to Figures 2a-2c but at Eastport (Gulf of Maine), where the
162 mean M_2 amplitude reaches up to 2.6 m. The significant differences between the sea level time
163 series are also dominated by nodal cycle (Figure 2f), as explain before. Table 1 shows the mean
164 values of M_2 tidal amplitude and EMD analyzed sea level magnitude (mode 1) at all sites after
165 the nodal cycle removed. The M_2 tidal amplitude varies from ~ 0.2 m (Baltimore, Key West, No
166 2 and 10 in Figure 1) to ~ 2.6 m (Eastport, No 8 in Figure 1). The mean values of EMD first
167 mode are coherent with that calculated from HA (Table 1).

168 The period of EMD mode 1 is shown in Figures 2b and 2d for tide gauge Wilmington and
169 Eastport (see Appendix Figure A2 for mode 2), respectively. At Wilmington/Eastport, the mean
170 periods of 12.97/13.01 and 24.34/24.23 hours of the first 2 modes are consistent with periods of
171 the semidiurnal and diurnal tide, respectively. The nodal cycle contributes to the differences
172 between the high frequency mean periods and semidiurnal/diurnal tides in all stations. Table 1
173 summarizes the mean periods of the EMD high frequency modes at all sites. The calculated
174 mean periods of EMD mode 1 and 2 are consistent with the periods of semi-diurnal and diurnal
175 tides at most of tide gauges, respectively (see discussion below on the more peculiar results at
176 Newport).

177 Comparison between Fig. 2d with Fig. 2f also suggests a significant M_2 time amplitude
178 trend exists at Wilmington, which has been found in earlier studies (e.g., Müller, 2011). On the
179 other hand, it also implies the modulation of nodal cycle may different at the sites. The EMD
180 method could not provide the sea level variations at a given frequency. We estimate the
181 modulation of nodal cycle to M_2 tide amplitude in EMD mode 1 with Eq. (2). The results are

182 overlaid in Fig. 2c and 2f for Wilmington and Eastport, respectively. The nodal cycle
183 modulations of 0.7 cm and 6.0 cm are referred to the M_2 tide amplitudes of 0.61 m and 2.75 m at
184 the two sites. The modulations of nodal cycle are also listed in Table 1. The amplitude of nodal
185 cycle estimated from EMD mode 1 varies from 1 cm to 6 cm at the sites (~ 2-3% of EMD
186 derived mean amplitude in Table 1). Compare with M_2 tide amplitude, the signal is high at
187 Baltimore (9%) and Key west (7%), which may relate to the instrument change at the sites (see
188 discussion below on the more peculiar results at the sites). Note the signal has been removed to
189 calculate the HA and EMD mode 1 mean M_2 tide amplitude (Table 1).

190 Figure 3 shows the variations of M_2 amplitude estimated from the HA and the EMD
191 methods at all selected stations. The nodal cycle and mean values in Table 1 have been removed
192 at each tide gauge and the correlation coefficients between the time series are listed in the table.
193 The correlations are higher than 0.6 at most of the sites and reach up to ~1.0 at Wilmington
194 (which shows the largest increase in tidal amplitude of any station). Low correlations are
195 presented at Atlantic City and Sewells Point (Norfolk) and the lowest correlation observed at
196 Newport. The Atlantic City station faces the open Atlantic Ocean, so that the magnitude of sea
197 level variations in the EMD first mode maybe affected by coastal or offshore ocean circulation
198 changes. Clear shifts in amplitude and phase of tidal constituents may attributes to small changes
199 in tide gauge location or surrounding coastal morphology (Mawdsley et al., 2015). Both the
200 Newport and Sewells Point locate inside the harbors, and harbor alteration impact the variations
201 of tidal constituents (Jay, 2009). The mean periods of EMD mode 1 and 2 show high
202 discrepancies with the periods of semidiurnal and diurnal tide at Newport. Notes the M_2
203 amplitude jumps at Baltimore and Key West in 1960-1970 and the EMD show stronger sea level
204 variations than HA, which could be related to changes in the tide gauge instruments, e.g., there

205 was a reported tide gauge instrument exchanges in 1967 at Key West. Significant variations in
206 the calculated period of sea level are shown at that time period, when the mean periods of 11.98
207 and 20.02 in EMD mode 1 and 2, respectively, were found. At Pulaski, the data gaps in 1974 is
208 also due to the tide gauge instrument change, which captured by the two approaches. At
209 Fernandina, the jump in the M_2 amplitude in 1905 are shown in the two methods, which are not
210 reported in existing publications. Consist with Müller et al. (2011), high temporal M_2 amplitude
211 variability presented with the two methods is coherent in the Gulf of Maine (Eastport, Portland
212 and Boston). Strong variability is also shown in the South Atlantic Bight (Charleston, Fernandina
213 and Pulaski). The stations at the Mid-Atlantic Bight region demonstrate relatively lower
214 temporal M_2 amplitude variability, with the M_2 amplitude decreasing in the Chesapeake Bay
215 (Chesapeake Bay Bridge Tunnel, Kiptopeke and Sewells Point) and in the Delaware Bay (Lewes)
216 from HA. The phase lag of 1 year between EMD and HA analysis is shown at Kiptopeke. The
217 correlation increases from 0.63 to 0.90 when the phase lag is adjusted in the time series.

218 In order to further evaluate the robustness of the results, an independent OTIS (Oregon
219 State University Tidal Inversion Software) regional tidal solution for the U.S. East Coast
220 ($1/30^\circ \times 1/30^\circ$) are used to calculate the M_2 amplitude from HA and EMD methods. The model
221 assimilated Topex/Poseidon, Topex Tandem and ERS data. The M_2 amplitudes are generated
222 with the Oregon State University Tidal Prediction Software (OTPS, Egbert and Everofeva, 2002)
223 and listed in Table 1. Although half of the sites are out of the model grid or on land, high
224 agreements are observed between EMD/HA and model derived M_2 tide amplitudes. At Eastport,
225 M_2 amplitudes of 2.64 m, 2.75 m and 2.77m are obtained from the HA, EMD and model solution,
226 respectively. Notes high discrepancies at Lewes and Sewells Point may attribute to the locations
227 of the sites.

228 **4. Discussion and summary**

229 The EMD/HHT has been widely used for various geophysical data. The HA is one of the
230 most popular method to investigate the changes in tidal properties (e.g., Mawdsley et al., 2015).
231 This study is possibly the first test that tries to adopt the EMD technique to describe the M_2
232 amplitude variability using the hourly tide gauge records; the results show high consistency with
233 the results estimated with the HA method and the independent OTIS regional tidal solution for
234 the U.S. east coast. Compared with HA, the advantage of the EMD over fitting methods is that it
235 is more general and can systematically filter out oscillating modes with unknown and variable
236 frequencies. Also, there is no need to perform multiple HA calculations on small subsections
237 (which reduce the accuracy compared with calculations of longer records), and instead, the
238 whole record is analyze at once. The EMD could also provide additional information on the
239 frequency of storm surges or other variations in sea level on different time scales from weekly to
240 decadal, though here only the highest modes relating to the main tidal cycles where analyzed.

241 The difference between the EMD and HA derived M_2 amplitude evolution is dominated
242 by the nodal cycle, which is captured by the EMD analysis mode 1. The nodal cycle significant
243 contribute to regional coastal changes (e.g., Gratiot et al., 2008) and impact coastal high tidal
244 levels (Haigh et al., 2011). Accounting of global median amplitude of 2.2 cm nodal cycle is
245 crucial to accurately estimate regional SLR (Baat et al., 2012). The EMD method demonstrates
246 nodal cycle modulations of about 2-3% (e.g., 1 - 6cm) of M_2 tide amplitude at the selected tide
247 gauges along the U.S east coast. The magnitude is consistent with findings based on equilibrium
248 tide expectation (Fig. 1b of Haigh et al., 2011). The comparison implies that indeed, the long
249 nodal cycle can affect tidal analysis if not explicitly removed.

250 Since the extremely slow changes of the astronomical forcing, tides are usually thought
251 of as stationary (Jay, 2009). So changes in tidal characteristics over time are usually associated
252 with local changes in morphology and tidal currents. In most cases, the changes are not fully
253 understood and may be region-dependent (Woodworth, 2010), as the physical processes cause
254 the tidal variations are complicated (Ray, 2006; 2009), particularly along the coast and on the
255 continental shelves (Müller, 2011; 2012). In addition to morphological changes and SLR that
256 affect the propagation pattern of tidal currents (which depend on water depth and the shape of
257 coastlines and bays), the changes in mixed layer depth caused by the warming of the upper ocean
258 layer may induce additional unknown baroclinic changes in currents. In the Gulf of Maine for
259 example, some small changes in topography or water properties can cause significant changes in
260 the large tides due to the high resonant state of the M_2 tide (Greenberg et al., 2012; Mawdsley et
261 al., 2015).

262 The Chesapeake and Delaware Bays show high rates of relative SLR (Ezer and Corlett,
263 2012; Ezer and Atkinson, 2014) and they have very different tidal characteristics than the Gulf of
264 Maine. The uneven vertical land subsidence (-1.90 mm/yr at Kiptopeke, -1.33 mm/yr at
265 Chesapeake City and Baltimore, -2.61 mm/yr at Sewells Point and up to -3.34 at Chesapeake
266 Bay Bridge Tunnel; (Zervas et al., 2013) contributes to uneven local SLR rates (Santamaría-
267 Gómez et al., 2012). In addition, the shape of estuaries and bays can affect the change in tidal
268 amplitude, as shown by the numerical simulations of Lee et al. (2016), who concluded that tidal
269 ranges and tidal energy in Delaware Bay and Chesapeake Bay will change differently under
270 higher sea levels when low-lying regions (5 m) are allowed to flood. The changes of estuarine
271 geometry and high sea levels may be responsible to the observed M_2 amplitude decrease in the

272 lower Chesapeake Bays (Kiptopeake to Sewells Point in Figure 3), which are in agreement with
273 the numerical experiments in Lee et al. (2016).

274 At Wilmington, both HA and EMD analysis demonstrate similar significant increase in
275 the M_2 amplitude due to morphological changes at the river where the tide gauge is located, as
276 previously reported (Ezer and Atkinson, 2014). Consistent with the study of Müller (2011), in
277 the South Atlantic Bight, the M_2 tidal amplitude increased at Charleston until ~1980 and then
278 remains flat (Ray, 2006). The other two tide gauges (Fort Pulaski and Fernandina) also show
279 notable M_2 amplitude variability with a negative offset after 1980 with the removal of trend
280 during 1930-1980, which might be associated with response to decadal variability in the Atlantic
281 Ocean. The vertical land subsidence is also notable at the sites (-1.24 mm/yr at Charleston, -1.36
282 mm/yr at Pulaski, -0.60 mm/yr at Fernandina from tide gauge records in the period from the
283 starting year to 2006, (Zervas et al., 2013)). In Miami Beach, Florida, tidal flooding events
284 increased by more than 400% after 2006 (Wdowinski et al., 2016). Hence, the variability of tides
285 should be considered in future regional sea level projections and evaluation of flood risks, since
286 an increase in tidal amplitude (by either sea level rise or local morphology change) would
287 increase the risk of tidal flooding (Ezer and Atkinson, 2014). Furthermore, changes in the tide
288 should not be neglected for implementing sea level rise mitigation and adaptation measures.

289 Global changes in tidal properties may have large spatial variations since different
290 mechanisms may dominate different coasts. Recent studies highlight the fact that tidal
291 propagation in shallow waters are modified by mean SLR, intensifying coastal threats at some
292 locations (e.g., Li et al., 2016). Furthermore, Müller et al. (2011) lists other possible reasons for
293 the tidal trend, e.g., variations in atmospheric dynamics and changes in the ocean circulation.
294 The bathymetric changes, e.g., increased depth and width caused by dredging and channel

295 modification, can cause long-term changes to the magnitudes of storm tides within harbors and
296 Estuaries (Orton et al., 2015). In New York Harbor (e.g, the Battery station), significant change
297 in storm tide magnitudes have occurred since 1840s. It is attributes to local changes to
298 bathymetry and the interannual variability in storm tides, which anticorrelated with NAO (North
299 Atlantic Oscillation) index (Talke et al., 2014). At Wilmington, increased channel depths are the
300 primary cause of altered tide range (Familkhalili and Talke, 2016).

301 The variations in AMOC and the GS contribute to the regional sea level variations on
302 multi time scales (e.g., Ezer, 2015; Ezer et al., 2013, 2016; Hakkinen, 2001; Han et al., 2016;
303 Lorbacher et al., 2010; Yin and Goddard, 2013), so a period of months to few years of higher
304 than normal sea level can also be accompanied by interannual variations in tidal amplitudes, as
305 seen here. Variations in GS transport produce variations in sea level gradient across the entire GS
306 length and this large-scale signal is then transmitted into the shelf by the generation of coastal-
307 trapped waves (Ezer, 2016). However, the exact mechanism of how changes in offshore currents
308 such as the GS and changes in wave field may affect the tidal variability over the different
309 regions, will require further research.

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320

321 **Appendix**

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323 Figure A1 here

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326 Figure A2 here

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491 **Captions:**

492 Table 1. Details of the selected Hourly Sea-Level Data (CBBT: Chesapeake Bay Bridge Tunnel,
493 Norfolk: Sewells Point). For each site, the columns 1-9 are name of the site, latitude (Lat) and
494 longitude (Long), start year of the data (end in 2016), the mean of M2 tide amplitude (Amp., m)
495 estimated using harmonic analysis (HA), mean magnitude of EMD analysis mode 1 (m) and the
496 removed modulation of nodal cycle (Nodal, m) using Eq.(2), M2 tide amplitude (m) estimated
497 from East Coast of America model with the Oregon State University Tidal Prediction Software
498 (OTPS, ‘*’ denotes the site is out of model grid or on land), correlation coefficient between HA
499 and EMD analysis derived variations of M2 tide amplitude (Fig.3) and the mean periods (h) of
500 EMD analysis modes 1 and 2, respectively.

501 Figure 1. Bathymetry of the study area and location of the selected tide gauges (the numbers
502 according to the tide gauges listed in Table 1). The regions with water depth larger than 1000 m
503 are marked as grey.

504 Figure 2. (a) Hourly sea level time series estimated with EMD analysis (the first mode, m) at
505 Wilmington. The Black curve denotes the M2 tide amplitude computed with harmonic analysis
506 (UTide). The red curve denotes the sea level magnitude computed as the mean of peak absolutes
507 of EMD first mode. (b) Period (hour) of the sea level EMD analysis first mode. M2 tide period of
508 12.42 hour is marked in y-label. (c) The difference (black curve, m) between the sea level
509 variation magnitude and M2 amplitude calculated with EMD analysis (mode 1) and HA. The
510 dashed line is the nodal cycle estimated from EMD (mode 1) sea level variation (m) using Eq.
511 (2). (d-e) are similar to (a-c) but at Eastport.

512 Figure 3. Evolution of M₂ amplitude estimated using harmonic analysis (Black curves) and EMD
513 (red curves) method. The nodal cycle and the mean amplitude over the all available time period
514 at each site have been removed.

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516 Appendix Figure A1. The EMD/HHT analysis for the Baltimore sea level data (mode 1-19, mode
517 0 denote original tide gauge records).

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519 Appendix Figure A2. Sea level variations of EMD mode 2 and according periods at (a) Eastport
520 and (b) Wilmington. K1 tide period of 23.93 hour is also shown.

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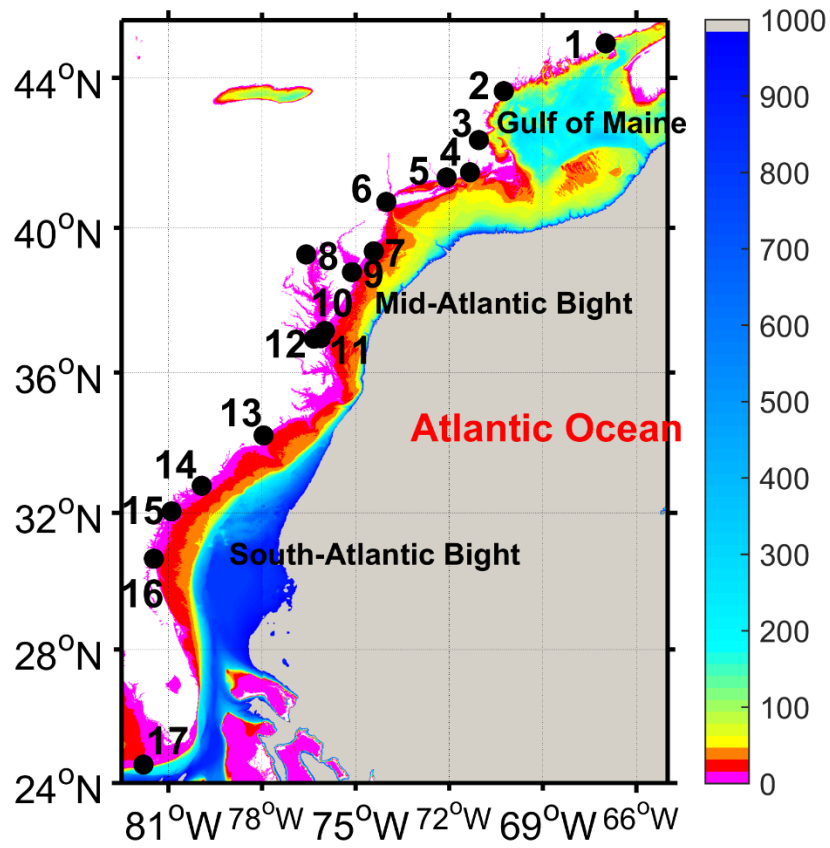
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534 (OTPS, ‘*’ denotes the site is out of model grid or on land), correlation coefficient between HA
535 and EMD analysis derived variations of M₂ tide amplitude (Fig.3) and the mean periods (h) of
536 EMD analysis modes 1 and 2, respectively.

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Name (State)	Lat. (°)	Long. (°)	Start year	HA Amp.	EMD/ Nodal	OTPS (EC)	Correlation (r)	Periods (Mode 1/2)
1. Eastport, ME	44.90	-66.98	1929	2.64	2.75/0.06	2.77	0.94	13.01/24.23
2. Portland, ME	43.66	-70.25	1910	1.35	1.36/0.04	*	0.93	12.62/24.29
3. Boston, MA	42.36	-71.05	1921	1.37	1.43/0.04	*	0.81	13.06/24.17
4. Newport, RI	41.51	-71.33	1930	0.51	0.49/0.02	0.46	0.01	5.89/22.34
5. New London, CT	41.36	-72.09	1938	0.36	0.37/0.01	0.37	0.66	12.89/23.64
6. Battery, NY	40.70	-74.01	1920	0.66	0.67/0.03	0.70	0.89	12.95/23.76
7. Atlantic City, NJ	39.36	-74.42	1911	0.58	0.59/0.02	0.58	0.30	12.82/23.30
8. Baltimore, MD	39.27	-76.58	1902	0.15	0.11/0.01	*	0.82	10.78/17.61
9. Lewes, DE	38.78	-75.12	1919	0.60	0.61/0.02	0.47	0.76	12.75/24.09
10. Kiptopeke, VA	37.17	-75.99	1976	0.39	0.39/0.01	0.32	0.63	12.56/23.94
11. CBBT, VA	36.97	-76.11	1975	0.38	0.38/0.01	0.30	0.60	12.45/25.56
12. Norfolk, VA	36.95	-76.33	1927	0.36	0.36/0.01	0.21	0.41	12.56/23.96
13. Wilmington, NC	34.23	-77.95	1908	0.58	0.61/0.01	*	1.00	12.97/24.34
14. Charleston, SC	32.78	-79.93	1899	0.77	0.78/0.02	*	0.90	12.72/24.13
15. Fort Pulaski, GA	32.04	-80.90	1935	1.01	1.04/0.03	*	0.79	12.82/24.25
16. Fernandina, FL	30.67	-81.47	1898	0.88	0.90/0.02	*	0.90	12.80/24.28
17. Key West, FL	24.56	-81.81	1913	0.17	0.15/0.01	*	0.58	11.98/20.02

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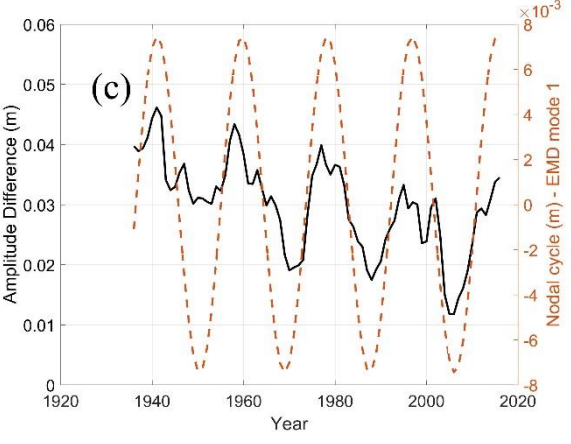
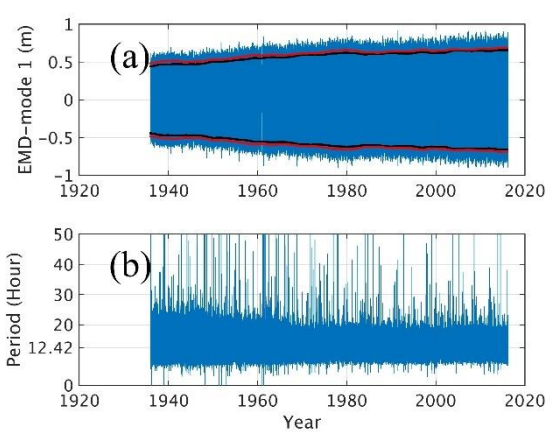
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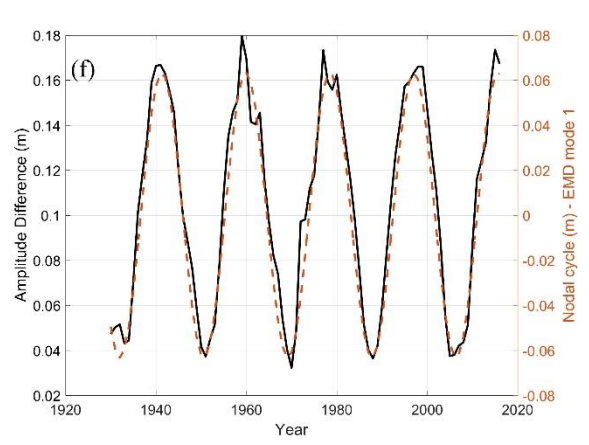
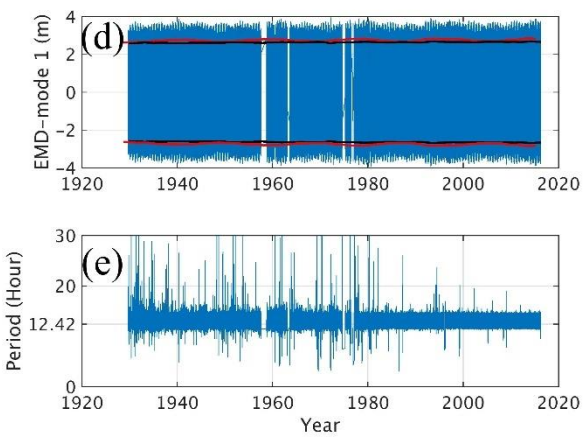
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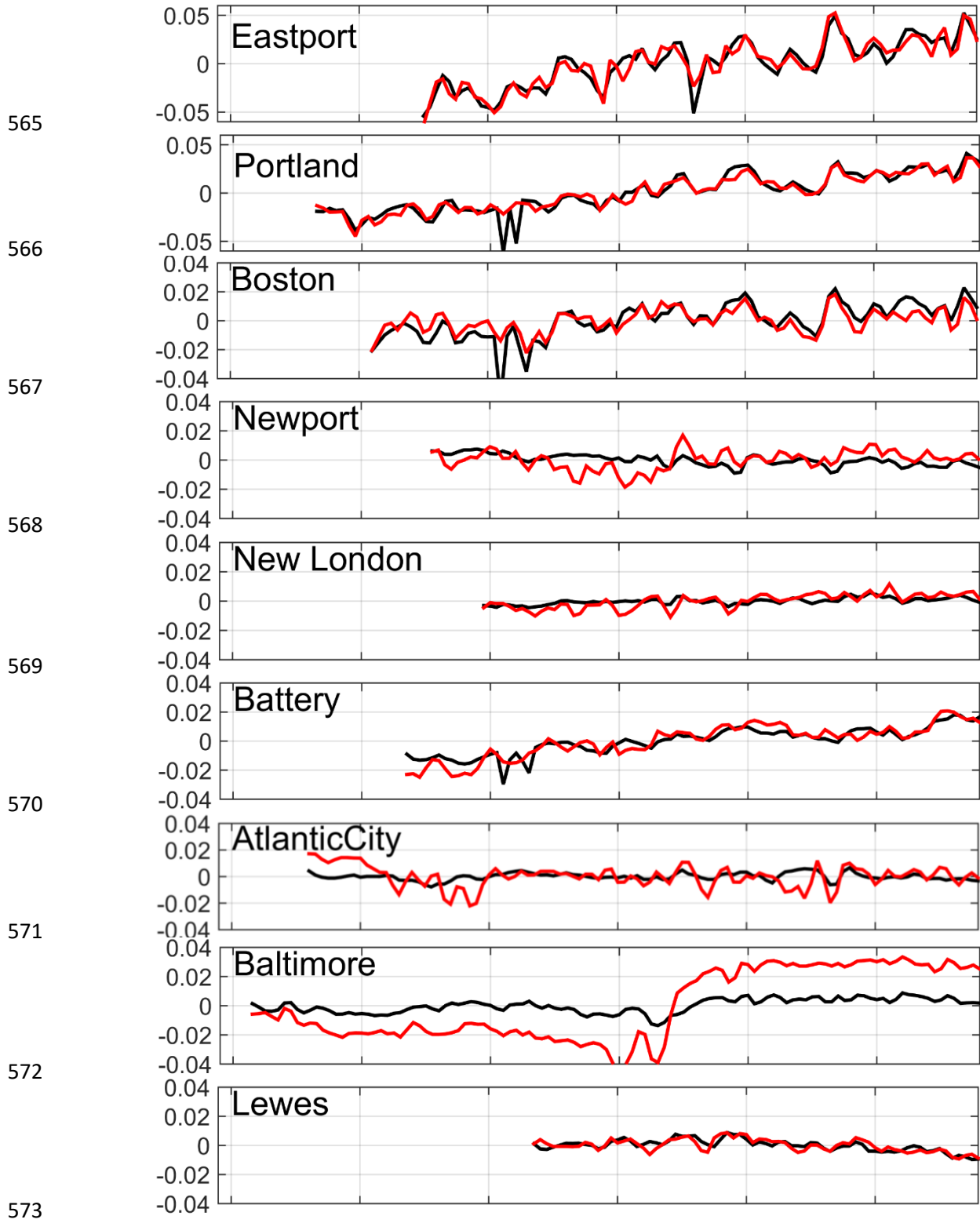
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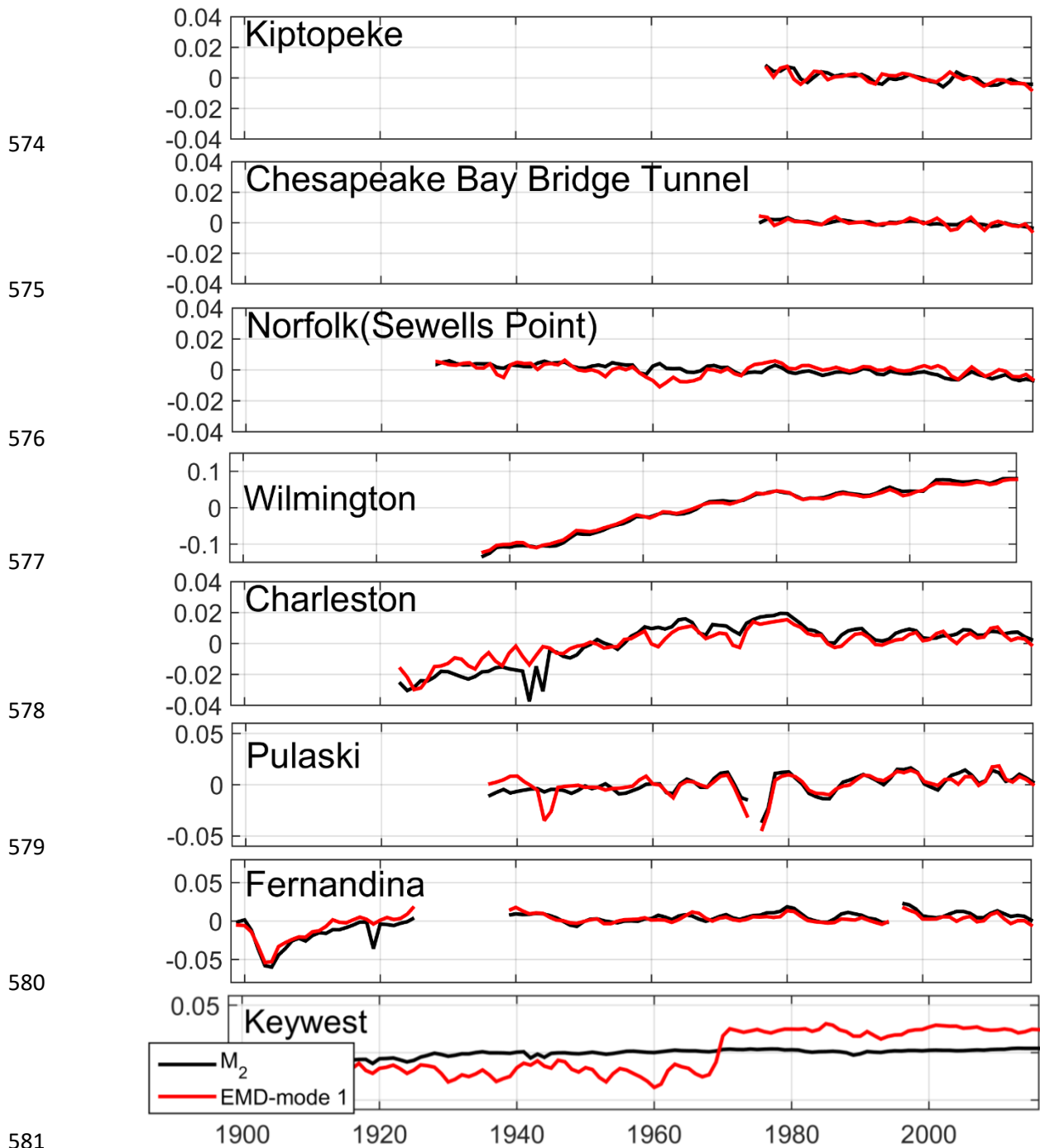
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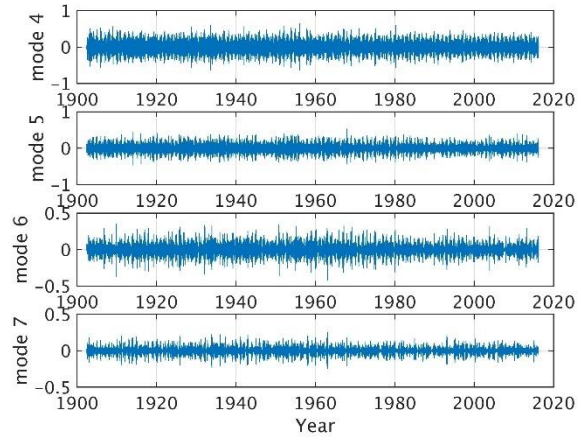
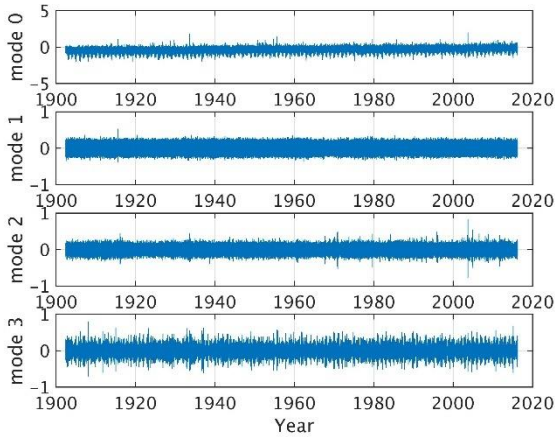
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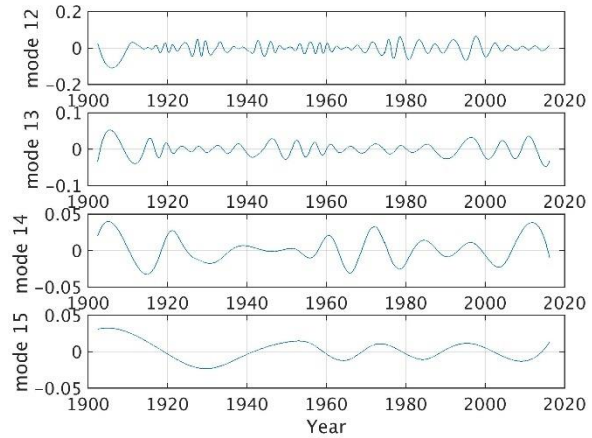
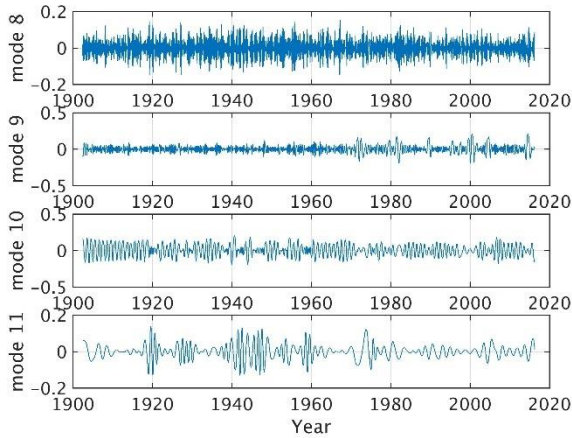




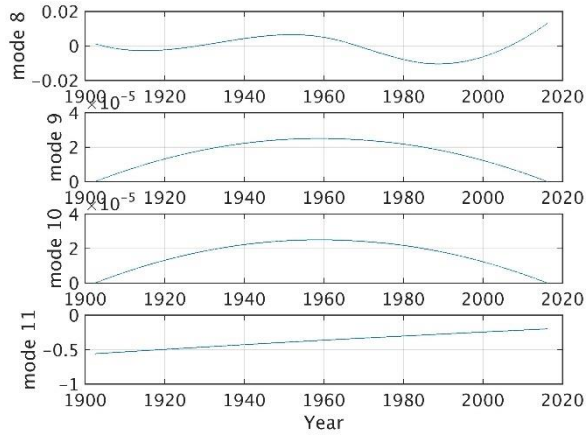
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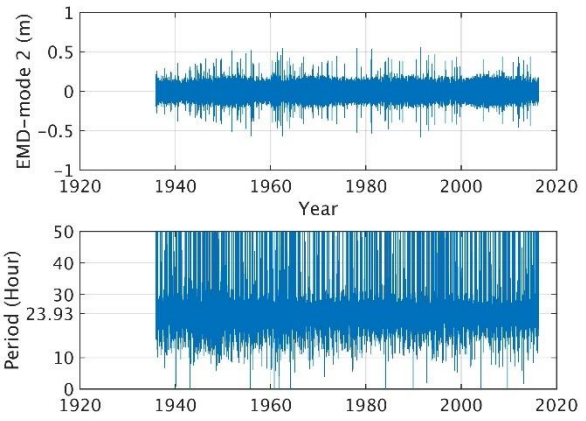
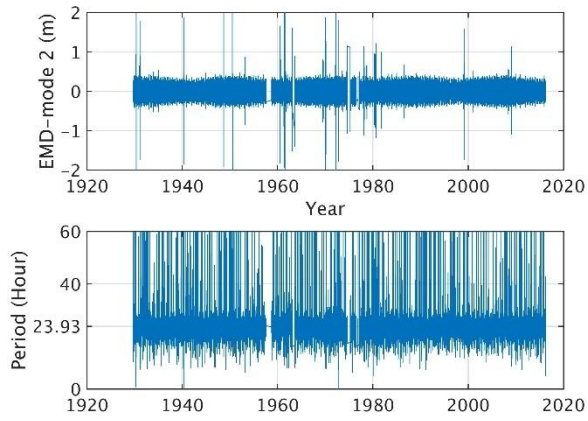
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